

$$P[X = x] = \frac{\Gamma(c) \lambda^x}{{}_1F_1(1; c; \lambda) \Gamma(c+x)} = \frac{(1)_x \lambda^x}{(c)_x x!} \frac{1}{{}_1F_1(1; c; \lambda)}$$