$$f_r = P\left[X = r\right] = \frac{(\rho)_k}{(a+\rho)_k} \frac{(a)_r (k)_r}{(a+k+\rho)_r} \frac{1}{r!}, \; r = 0, 1, ...$$